

# Residual Strain Development in Laminated Thermoplastic Composites Measured using Fibre Bragg Grating Sensors

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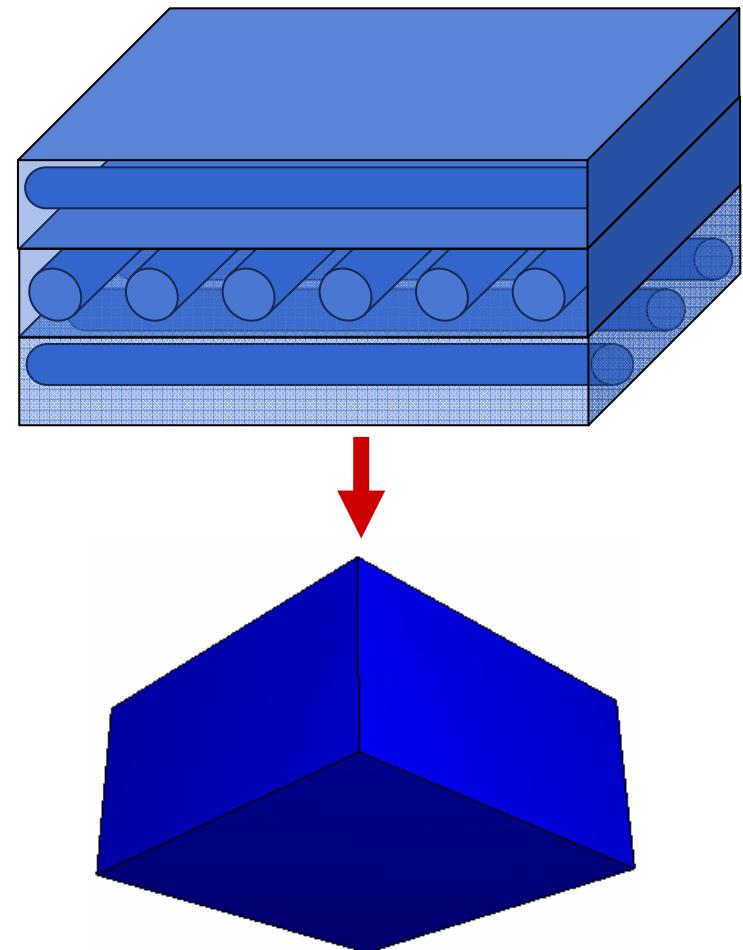
# Outline

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- Residual Strains in TP Composites
- FBG's for Residual Strain Measurements
- Fabrication and Measurement Procedures
- Experimental Results
- Modeling
- Conclusions and Perspectives

# Residual Strains in TP Composites

- CTE matrix  $\neq$  CTE reinforcing fibres
  - ➡ Micromechanical strains
- Anisotropic plies
  - ➡ Interlaminar strains
- Moulding pressure, temperature gradients
  - ➡ Global strains



Stresses During Cooling

# Motivation & Direction

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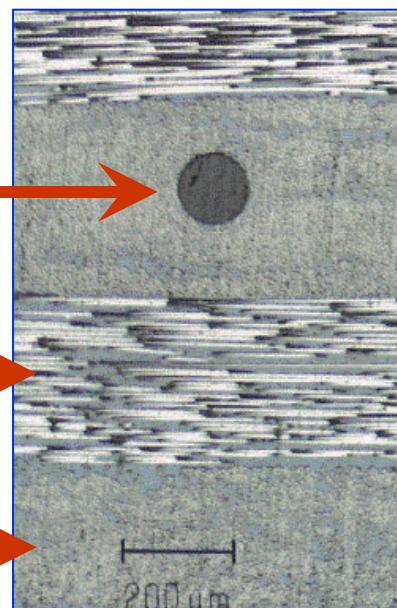
- Residual strains can be the source of damage initiation and premature failure in composites....

## **Objective:**

- Develop a method for direct internal strain measurements:
  - ▶ (residual stresses, process monitoring)

# Measuring the Internal Strain State

- How can we best measure internal residual strains?

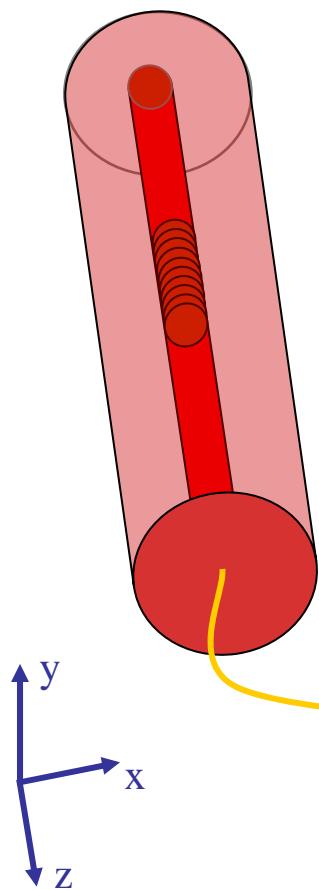


## Fibre Bragg Grating Sensors

- ➔ Minimal disruption of surroundings
- ➔ Precise location in given layers
- ➔ Sensitive to multi-dimensional and non-uniform strain fields

# Thermomechanical-Optic Relations

## Uniform Strain Field

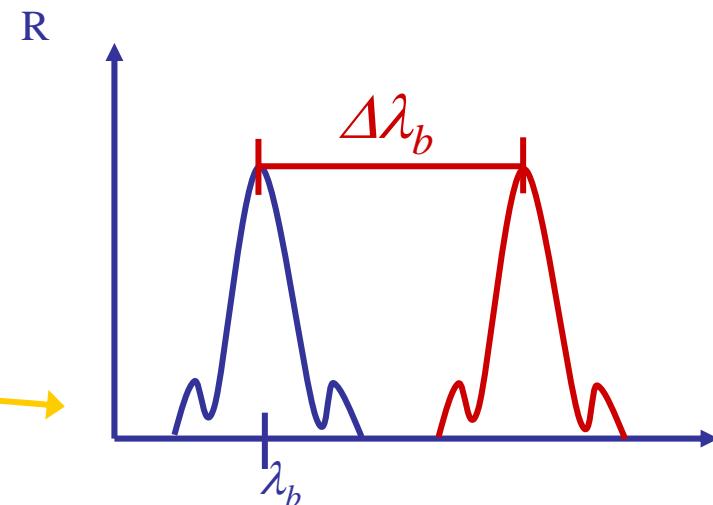


$$\frac{\Delta\lambda_b}{\lambda_b} = \varepsilon_z - \frac{n_0^2}{2} [p_{11}\varepsilon_x + p_{12}(\varepsilon_z + \varepsilon_y)] + \xi\Delta T$$

IF  $\varepsilon_x = \varepsilon_y = -v\varepsilon_z$  and  $\Delta T = 0$



$$\frac{\Delta\lambda_b}{\lambda_b} = (1 - p_e)\varepsilon_z$$



$n_o$	Effective Index of Refraction
$\varepsilon_i$	Normal Strain in i-Direction
$p_{11}, p_{12}$	Pockel's Constants
$\xi$	Thermal-Optic Coefficient
$\Delta T$	Change in Temperature

# $p_e$ Simplification Limitations

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- Consider the following cases:

• **Plane Strain**

$(\epsilon_z = 0)$

• Thermal Contractions

$(\epsilon_x = \epsilon_y \neq -v\epsilon_z)$

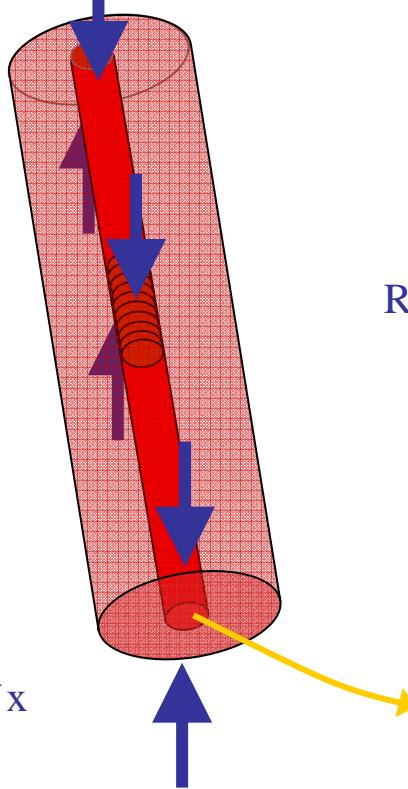
• Birefringence

$(\epsilon_x \neq \epsilon_y)$

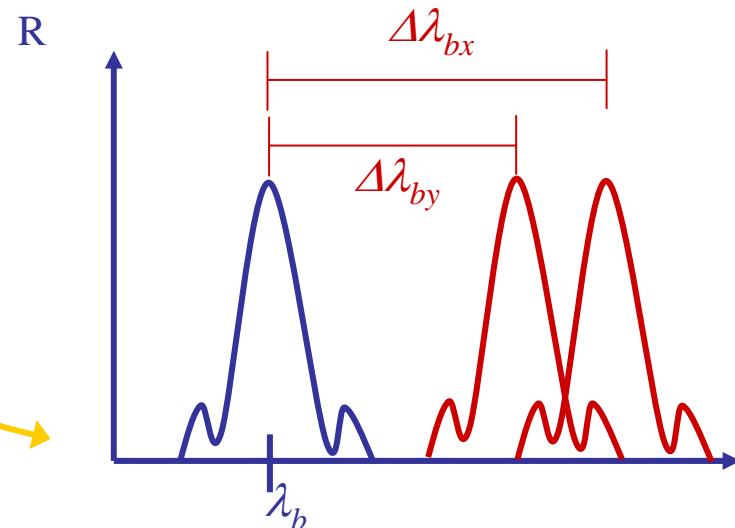
► Error depends on 3D strain state!

# Complete 3D Solution

Unequal  
Transverse  
Strains



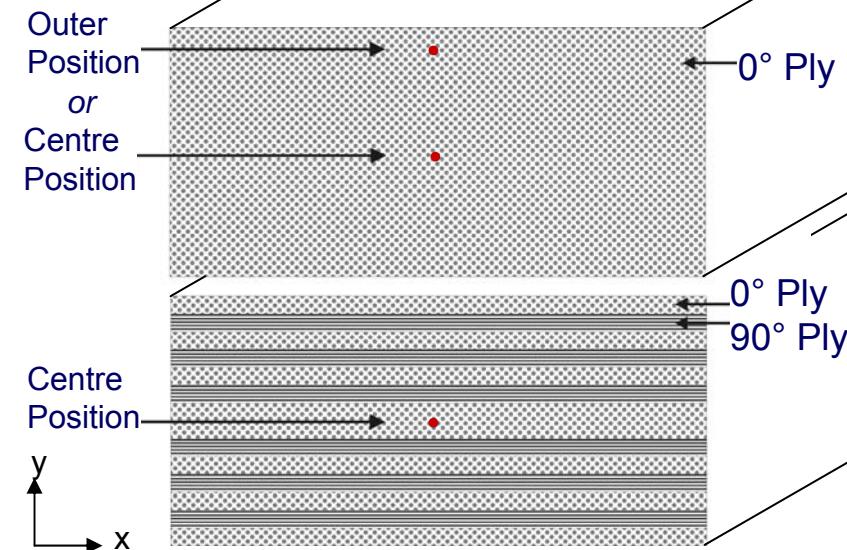
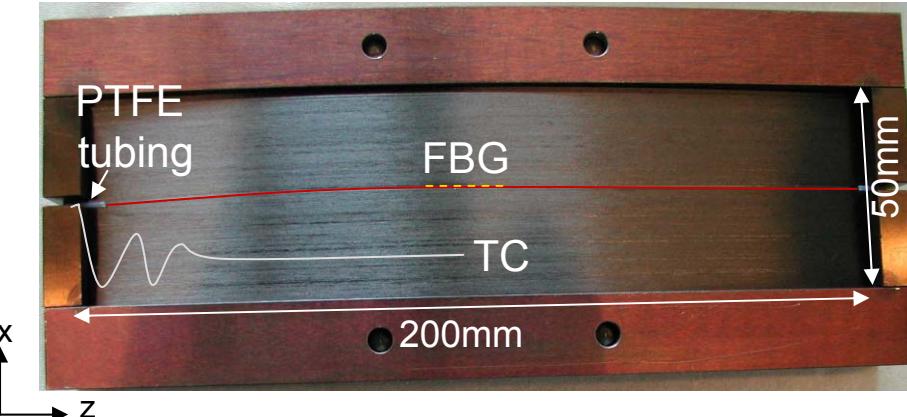
$$\frac{\Delta\lambda_{bx}}{\lambda_b} = \varepsilon_z - \frac{n_0^2}{2} [p_{11}\varepsilon_x + p_{12}(\varepsilon_z + \varepsilon_y)] + \xi\Delta T$$
$$\frac{\Delta\lambda_{by}}{\lambda_b} = \varepsilon_z - \frac{n_0^2}{2} [p_{11}\varepsilon_y + p_{12}(\varepsilon_z + \varepsilon_x)] + \xi\Delta T$$



2 Equations,  
3 Unknowns!

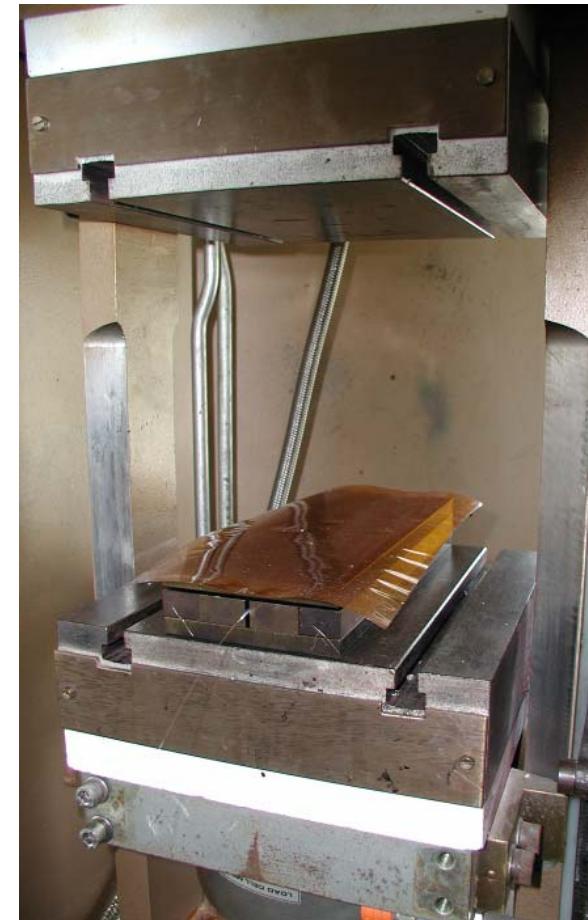
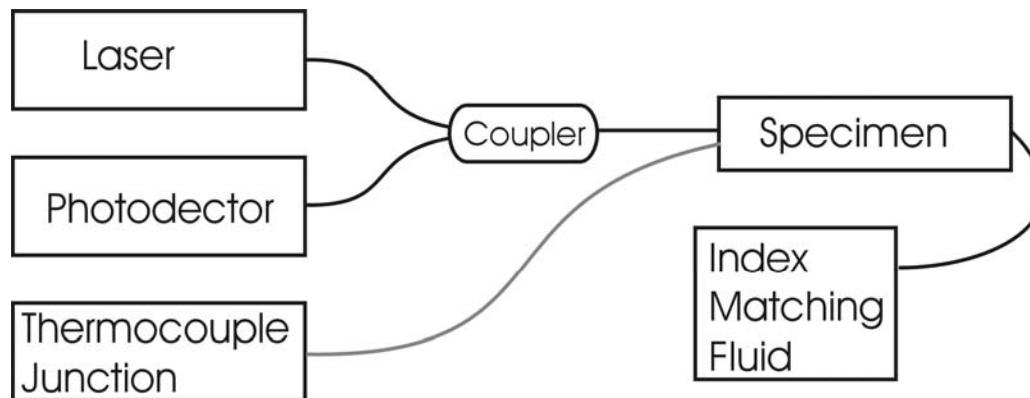
# Composite Specimens

- AS4/PPS prepreg
  - Unidirectional (UD) and Cross-ply (CP) laminates (28 plies)
- FBG sensors: 22mm gauge length, 1300nm
  - Coating removed past sensor length
- 250 $\mu$ m diameter thermocouple



# Consolidation Process

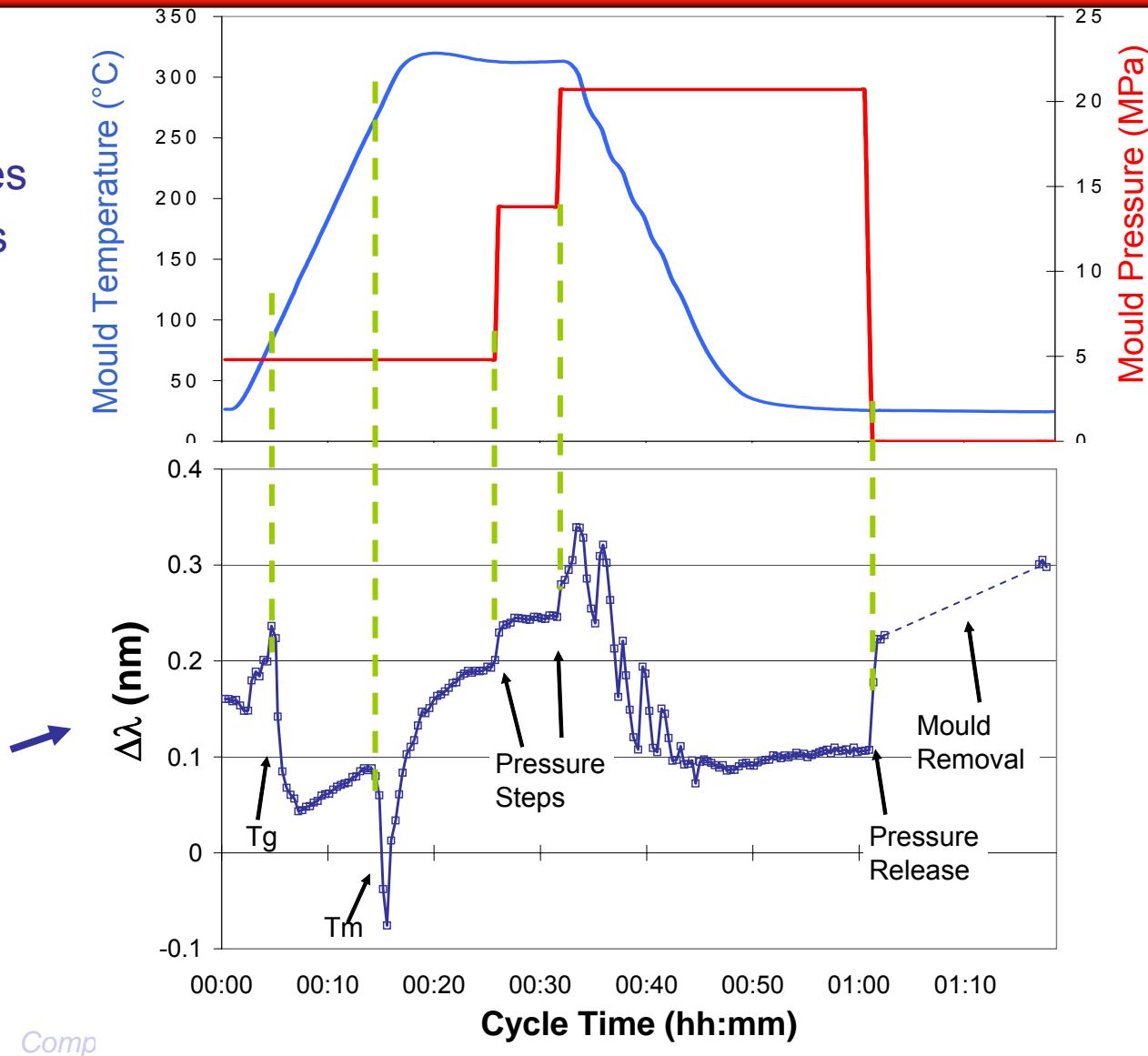
- Plies are compressed in hot press
- A polarized tunable laser probes the FBG
- Photodetector retrieves reflected spectra
- Thermocouple & FBG readings



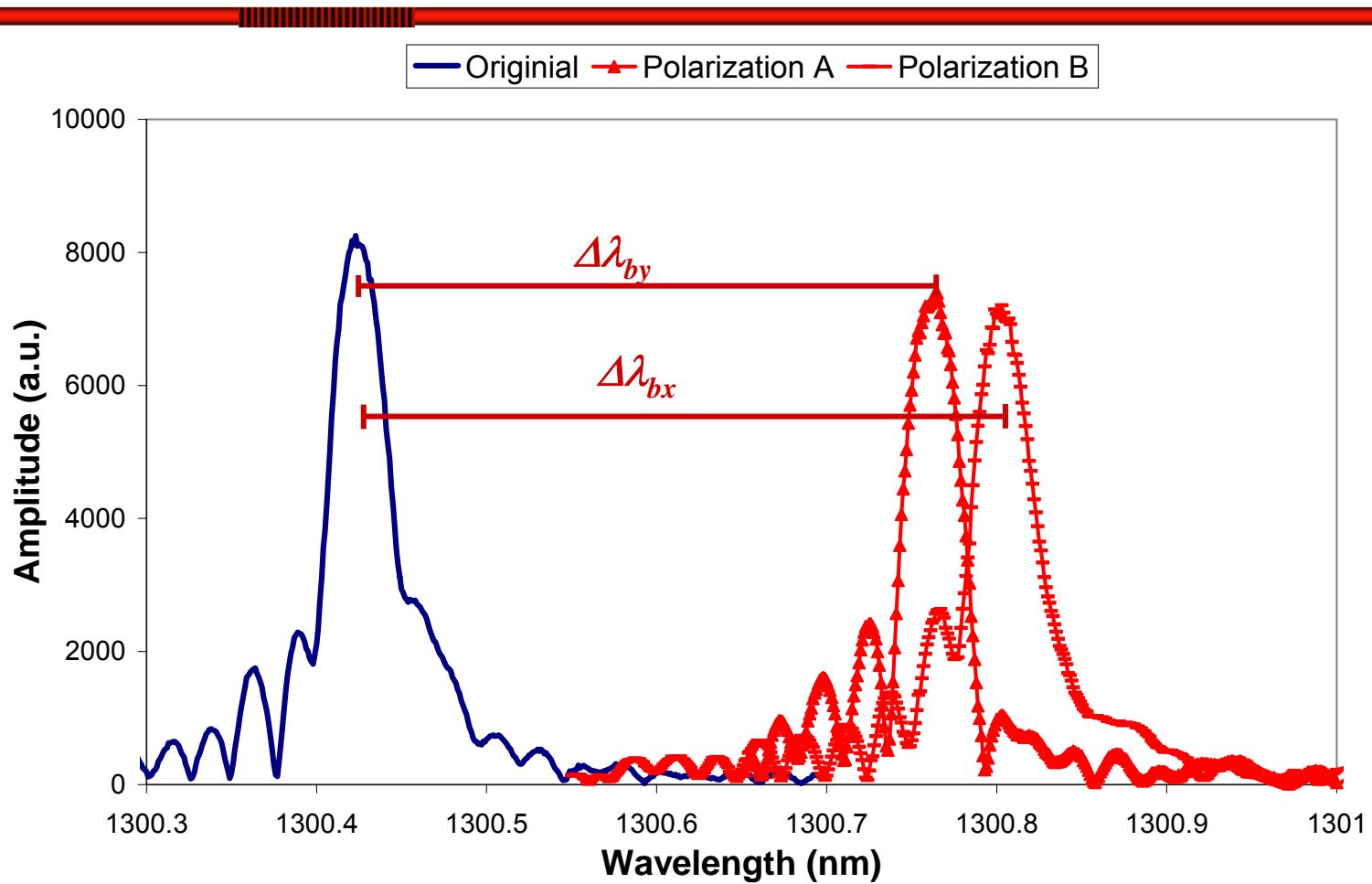
# Consolidation Process

- FBG responds to
  - Pressure changes
  - Material changes

Temperature Compensated  
Bragg Wavelength Changes



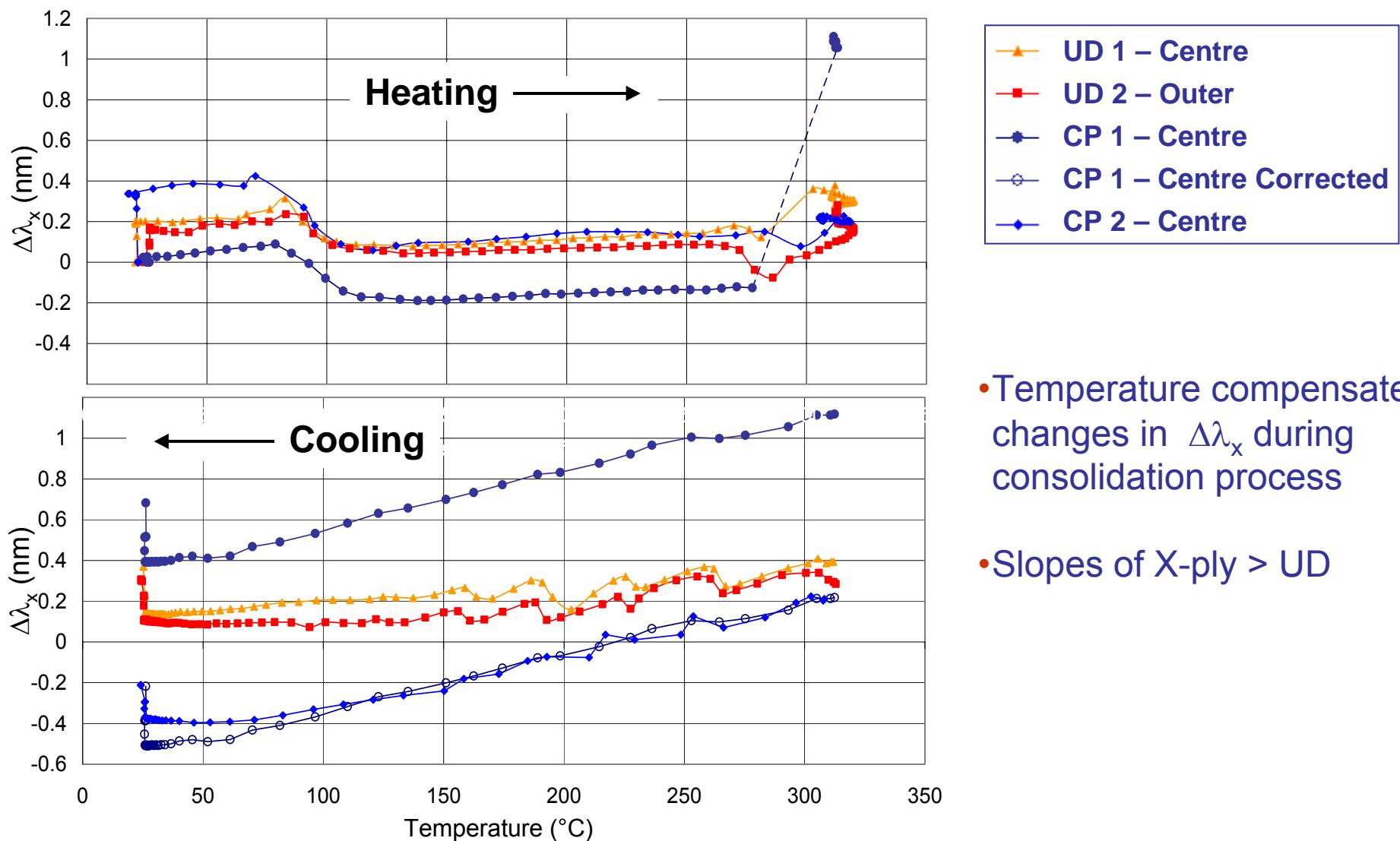
# Final Residual Strains – room temp



$$\frac{\Delta\lambda_{bx}}{\lambda_b} = \varepsilon_z - \frac{n_0^2}{2} [p_{11}\varepsilon_x + p_{12}(\varepsilon_z + \varepsilon_y)]$$

$$\frac{\Delta\lambda_{by}}{\lambda_b} = \varepsilon_z - \frac{n_0^2}{2} [p_{11}\varepsilon_y + p_{12}(\varepsilon_z + \varepsilon_x)]$$

# Changes in Bragg Wavelengths



# Modeling Considerations

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- What factors affect the internal strain state in the composite during consolidation?
    - Thermal expansion/contraction
    - Thermal gradients
    - Crystallization
    - Hot Press/ Mould forces frozen into laminate
    - Relaxation
- Material properties depend on local temperature!!

# Simplified Consolidation Model

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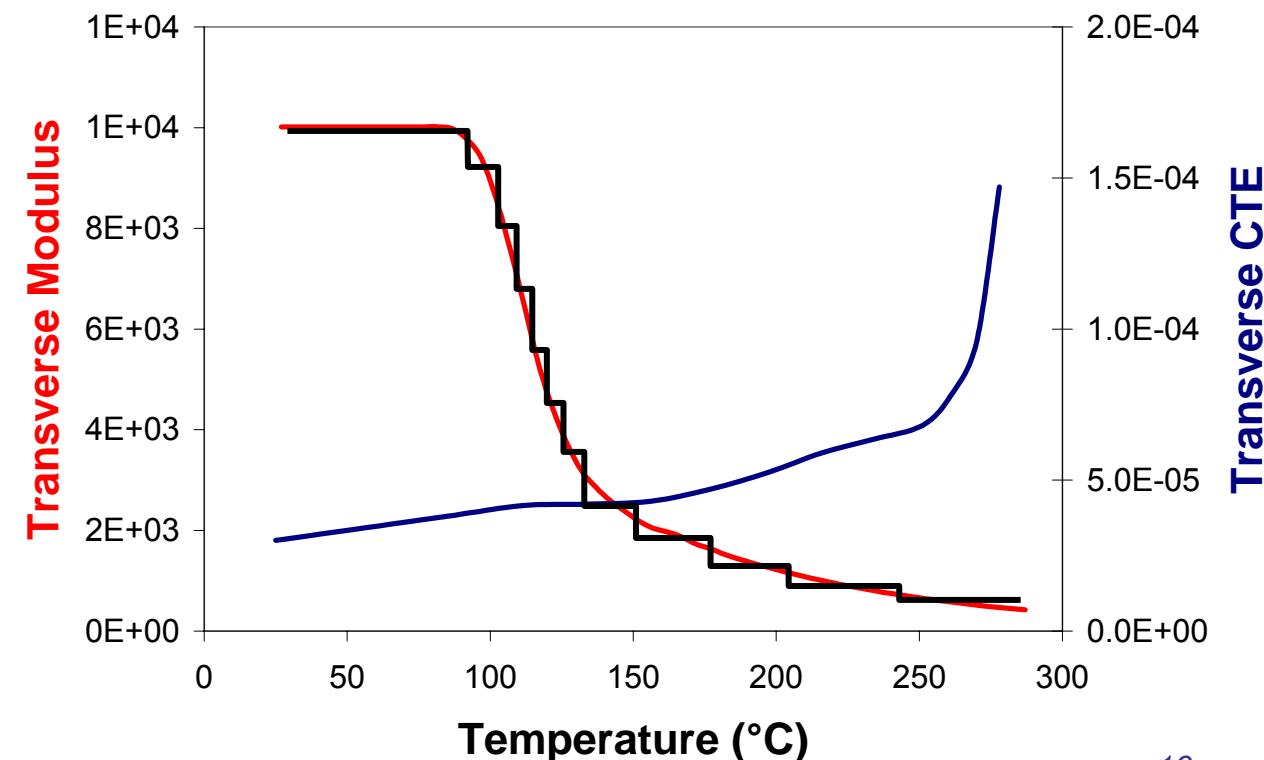
- Assumptions for a simplified model:
  - Generalized plane strain
  - Thermal contraction dominates
    - i.e. neglect crystallization effects
  - Negligible thermal gradients
  - Temp dependent polymer moduli and CTE
  - Stresses/strains accumulation can be divided into steps that will be summed

# Elastic Step Model

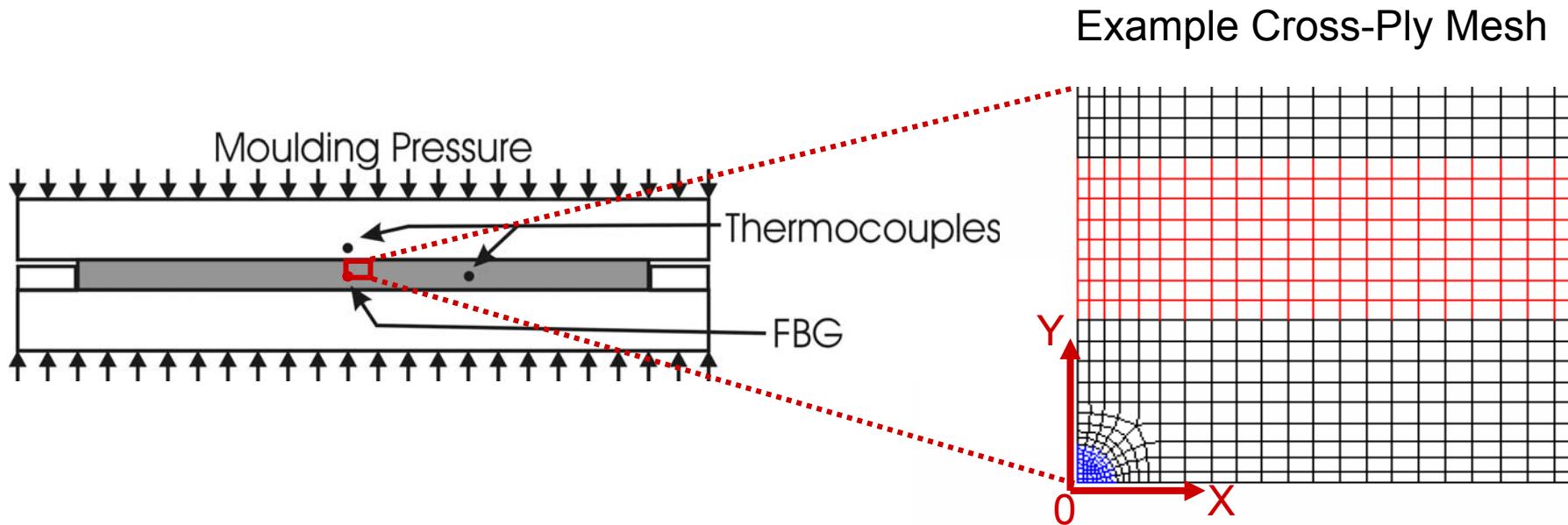
- Divide the cooling process into 13 steps
- Steps represent temperature ranges where material properties are piecewise constant

$$\varepsilon_{total_{ij}} = \sum_{k=1}^{13} \varepsilon_{ij}^k(T)$$

$$\sigma_{total_{ij}} = \sum_{k=1}^{13} \sigma_{ij}^k(T)$$



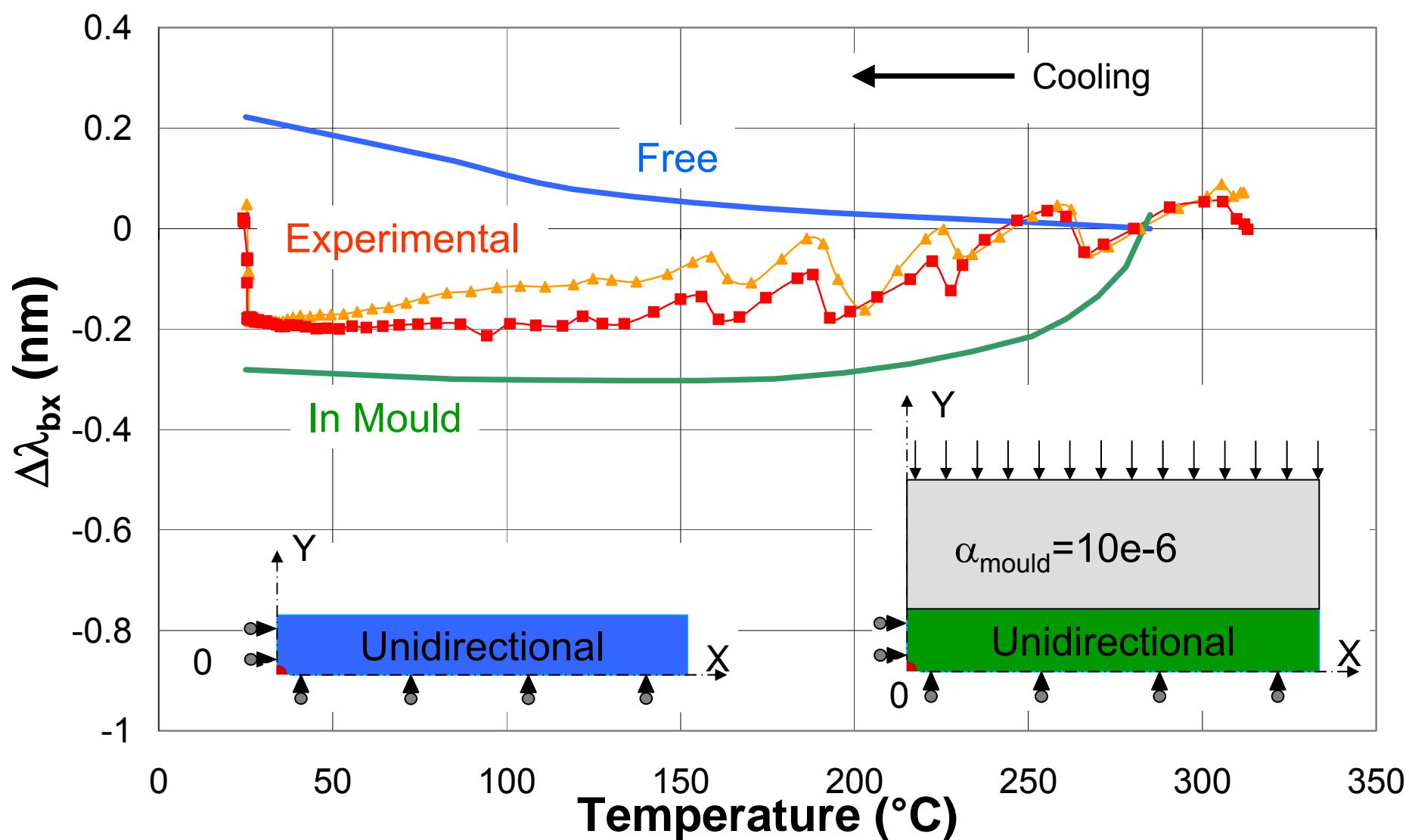
# FEM Model – Elastic Step Method



- $\varepsilon_x, \varepsilon_y, \varepsilon_z$  from fibre core are inserted into optomechanical equations


$$\Delta\lambda_b(\varepsilon_x, \varepsilon_y, \varepsilon_z)$$

# Evolution of $\Delta\lambda_{bx}$ During Cooling (Uni)



# Conclusions

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- FBG's are capable of registering changes in material state and moulding pressure
- During consolidation, residual strains accumulate at different rates according to lay-up
- Consolidation pressure & mould contact cause birefringence in FBG sensors
- Complete opto-mechanical relationships are required to use FBG measurements

# Future Perspectives

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- Improve the consolidation model that relates strains in the FBG with strains in composite
- Continue to improve methods to account for polarization/birefringence effects
  - ➔ Including a method to decouple non-uniform longitudinal strains from transverse strains

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